# A METHOD FOR ESTIMATING UNDRAINED CYCLIC STRENGTH OF SANDY SOILS USING STANDARD PENETRATION RESISTANCES

Fumio Tatsuoka\*, Toshio Iwasaki\*\*, Ken-ichi Tokida\*\*\*, Susumu Yasuda\*\*\*\*, Makoto Hirose\*\*\*\*\*, Tsuneo Imai\*\*\*\*\* and Masashi Kon-no\*\*\*\*\*\*

# ABSTRACT

In evaluating liquefaction potential of saturated sandy deposits, it is necessary to estimate undrained cyclic shear strength of soils. On many occassions in actual design procedures, it is very convenient if engineers can evaluate undrained cyclic shear strength of sandy soils with use of ordinary engineering properties of soils and grounds such as grading properties of disturbed samples and blow counts (N-values) by standard penetration tests. For this purpose, available data of sand sampling, dynamic triaxial tests on undisturbed specimens, N-values by standard penetration tests and gradings were analysed and a correlation among dynamic shear strength, mean diameter  $D_{50}$  and  $D_r^*=21\sqrt{N/(\sigma_v'+0.7)}$ , in which N is the blow counts by standard penetration tests and  $\sigma_{v'}$  is the in situ effective overburden pressure in kg/cm<sup>2</sup>, was obtained. This correlation is represented by a simplified equation. Using this equation, approximate dynamic shear strengths of reclaimed and alluvial sandy deposits can be easily estimated from N-values,  $\sigma_{v'}$  and  $D_{50}$ .

Key words:dynamic, earthquake resistant, grain size, laboratory test, liquefaction,<br/>penetration test, repeated load, sampling, sandy soil, soundingIGC:D6/C3/C6

# INTRODUCTION

In actual practical procedures for evaluation of liquefaction potential of sandy soil deposits, blow counts or N-values by standard penetration tests have often been utilized. Since standard penetration test is easy to conduct in situ, it is widely utilized in common engineering practices in Japan. At present, in designing most of civil engineering structures this test is generally conducted. Therefore, procedures to estimate liquefaction potential with use of N-values are convenient to practical engineers. However, it is also well-known that this test is rather crude to estimate precise soil properties.

- \* Associate Professor, Institute of Industrial Science, University of Tokyo, 22-1, Roppongi 7, Minato-ku, Tokyo.
- \*\* Chief, Ground Vibration Section, Public Works Research Institute, Ministry of Construction, 5-12-11, Anagawa, Chiba.
- \*\*\* Research Engineer, do.
- \*\*\*\* Research Engineer, Kisojiban Consultants, Co., Ltd.
- \*\*\*\*\* Research Engineer, Soil Laboratory, Toa Harbor Works Co., Ltd.
- \*\*\*\*\*\* Chief, Earthquake Engineering Division, Urawa Research Institute, OYO Corporation, Ltd. \*\*\*\*\*\*\* Engineer, OYO Corporation, Ltd.
  - Written discussions on this paper should be submitted before July 1, 1979.

44

#### TATSUOKA ET AL.

Therefore, for recent important structures to be constructed on liquefaction susceptible deposits, more sophisticated geological surveys are often conducted where undisturbed samples are secured and dynamic triaxial tests on undisturbed specimens are performed for precisely evaluating undrained cyclic shear strength. Since this procedure is rather expensive, it cannot be applied to the whole of a wide area of one big construction project. In this case, standard penetration tests should be performed for the whole area as a supplemental one. Also this procedure cannot be applied to a relatively small construction project.

Considering these situations, while there are much criticism to the standard penetration test, it is necessary and useful to develop a simplified empirical formula to estimate in situ dynamic shear strength in terms of N-values by standard penetration tests and other soil index properties for practical design purposes.

In this respect, it should be noted, however, that N-values are considerably sensitive to grain size. In general, N-values for clayey deposits are much smaller than those for sandy deposits and N-values for sandy deposits are also much smaller than those for gravelly deposits. From these facts, it can be anticipated that N-value of one soil may differ considerably from that of another soil even if the two soils have an equal dynamic strength. Therefore, it seems that if N-values are utilized without considering the effects of grain size on N-values, results of analyses can be quite misleading.

Reported herein is a method of evaluating undrained cyclic strengths of sandy soils in triaxial stress condition from standard penetration resistances N-values with taking into account the effects of grain size on N-values. From the dynamic shear strengths estimated by the method which is proposed in this paper, in situ dynamic shear strength for liquefaction potential analyses can be evaluated.

# TWO METHODS EXAMINED IN THIS STUDY

In most of previous studies, in situ dynamic shear strengths of sands for liquefaction potential analyses were evaluated using relative densities which were in turn estimated from measured N-values and effective overburden pressure  $\sigma_{v'}$  (Seed and Idriss, 1967). This method is denoted as the A-method in Fig.1. In the A-method, two different equations are utilized, those are (i) the relationship among N,  $\sigma_{v'}$ , relative density  $D_r$  and other soil and ground parameters, and (ii) the relationship among undrained cyclic strength,  $\sigma_{v'}$ ,  $D_r$ and other soil parameters. This method will be firstly examined in this paper. In the



Fig. 1. Comparison between A-method and B-method

second method which is denoted as the B-method in Fig. 1, undrained cyclic strengths are directly evaluated from measured N-values,  $\sigma_{v'}$ ,  $K_0$  and grading. In this method, a correlation equation among N-values,  $\sigma_{v'}$ ,  $K_0$ , grading and undrained cyclic strength is utilized. In this study, the second method was found to be more convenient and more precise than the A-method.

# EXAMINATION OF A-METHOD

The most important factor which is firstly evaluated in the A-method is relative density  $D_r$  defined as

$$D_r = \frac{e_{\max} - e}{e_{\max} - e_{\min}} \times 100 \quad (\%) \tag{1}$$

in which e is the estimated in situ void ratio and  $e_{\max}$  and  $e_{\min}$  are the maximum and the minimum void ratios of the soil, respectively.

In order to estimate in situ dynamic shear strength from the values of relative density which have in turn been estimated from measured *N*-values, it is necessary that the following three points be confirmed.

- (1) Relative density can be estimated from measured N-values within the limit of errors allowable for engineering purposes.
- (2) The standard methods of measuring the minimum and the maximum densities of sands have been established.
- (3) Dynamic shear strength can be estimated from estimated relative densities within the limit of errors allowable for engineering purposes.

To confirm item (1), a number of studies have been performed already. Among them, Meyerhof (1957) proposed a following empirical equation on the basis of laboratory tests using clean sands performed by Gibbs and Holtz (1957):

$$D_r^* = 21\sqrt{N/(\sigma_v' + 0.7)}$$
(2)

in which  $D_r^*$  is the estimated relative density (as distinguished from measured relative density  $D_r$  by Eq. (1)).

The almost identical one to Eq. (2) was utilized by Seed and Idriss (1967) in evaluating in situ relative densities of the sand deposits in Niigata city where soil liquefaction was observed widely during the Niigata Earthquake of 1964. Recently, Japanese Society of Soil Mechanics and Foundation Engineering conducted sand samplings at Kawagishi-cho (site H) using a modified Bishop-type sand sampler (JSSMFE, 1976; Bishop, 1948; Hanzawa and Matsuda, 1977). The liner had the inside diameter of 5.3cm and the length of 65cm. The liner was driven into the sand deposit with the position of the piston being fixed. For sampling, the liner was pulled up into the chamber filled with air, causing negative pore pressure and minimizing disturbance to the sample (see Table 1). In situ dry density  $\gamma_d$  was estimated by the equation

$$\gamma_d = \frac{W_s}{Al - \Delta V} \tag{3}$$

in which A, l and  $\Delta V$  are inside cross-sectional area of the liner, the length of insertion of the liner and the volume of the lost sample and  $W_s$  is the dry weight of the secured sample. Void ratio determined by this procedure will be denoted as  $e_F$  hereafter.  $e_{\min}$  was determined by tamping a mold using air-dry sand applying the pressure of  $1 \text{ kg/cm}^2$  on the top.  $e_{\max}$  was the average of two values by two methods (Kolbuszewski, 1948; Tanimoto, 1975).  $e_{\min}$  and  $e_{\max}$  of Toyoura Sand by these methods are 0.60 and 0.94, respectively. Figs. 2 and 3 show the comparisons between measured relative density  $D_r$  and estimated relative density  $D_r^*$  by Eq. (2). As Castro (1975) did, the standard penetration



resistances corresponding to undisturbed samples which are referred to in this paper were obtained either in adjacent borings at the same elevation or directly above or below undisturbed samples in the same boring and the blow count (*N*-value) was not considered representative of the undisturbed sample if the soil description or grain size, or both, were different.

The sand deposit at Kawagishi-cho consists of relatively clean medium grain sized sand. While a scatter is observed in the data in Fig. 2 the correlation between  $D_r$  and  $D_r^*$  is not bad. And it is evident that Eq. (2) may be used for such grounds if errors of 15 percent in relative density can be allowed. It is also worthy to note from Fig. 3 that for sand including 5 percent or more gravel,  $D_r^*$  is larger than  $D_r$ . This means that for gravelly deposits, Eq. (2) is misleading. On the other hand, Fig. 4 shows another comparison between  $D_r$  and  $D_r^*$  for fine sands whose  $D_{50}$  are smaller than 0.3mm. The method for sand sampling at this site (site A) is identical to that adopted by JSSMFE (1976). Site A along Tokyo Bay consists of hydraulically filled deposits and alluvial sandy deposits which are located under the hydraulic fills.  $e_{\min}$  and  $e_{\max}$  were determined by the method of Yoshimi and Tohno (1972).  $e_{\min}$  and  $e_{\max}$  of Toyoura Sand determined by the authors following the Yoshimi-Tohno method are 0.64 and 0.96, respectively (see Table 1). It can be seen in Fig. 4 that for these fine sands, Eq. (2) underestimates the relative densities and is quite misleading especially for sands with smaller grain size. It is to be noted that such underestimations in the relative densities of saturated fine sands by Eq. (2) as shown in Fig. 4 has also been indicated by the experimental data by Gibbs and Holtz (1957), while the date is not shown here.

Fig. 5 shows another comparison between  $D_r$  and  $D_r^*$  at site B along Setonaikai Sea in Shikoku where sand samplings were performed with use of a twist sampler (Ogura et al., 1978). The surface deposit at site B is a hydraulic fill and beneath this there is an alluvial sandy deposit. The liner is 7.0cm in inner diameter and 80cm in length. This is a double tube thin wall sampler where sealing between the piston and the liner is designed to be perfect. Identically to the modified Bishop-type sand sampler, the position of the piston is kept fixed when the liner is driven into sand deposits. When driving is completed, the inner liner is pulled up 7cm to make room between secured sample and sand deposit. Then only the inner liner is twisted with the outer liner being kept fixed. This is for the pre-equipped rubber tube to cover the bottom face of the secured sample by twisting. This rubber tube is equipped in advance at the bottom between the outer liner and

the inner liner. With this procedure, secured sample is protected for dropping from the liner. Void ratios for estimation of in situ relative densities were averaged values in the liners before freezing. These void ratios will be denoted as  $e'_{F}$  hereafter. These liner and secured samples were frozen at the site with use of dry ice after pulling the apparatus to the ground surface as carefully as possible.  $e_{\min}$ and  $e_{max}$  were determined by the Yoshimi-Tohno method. It can be seen in Fig. 5 that also for this site, Eq. (2) underestimates relative density for finer sands. Fig. 6 shows a summarized relationship between  $D_r - D_r^*$  and  $D_{50}$ for several sites. Ishihara (1976, 1977) and Ishihara and Silver (1977) performed sand samplings at a hydraulic fill and an alluvium deposit beneath





the hydraulic fill along Shinano River in Niigata city (site C) using a large diameter sand sampler (20 cm in inner diameter and 100 cm in inner height). Void ratios for estimation of in situ relative densities were measured for triaxial specimens which were confined by the vacuum pressure of  $-0.2 \text{ kg/cm}^2$ . The values of void ratios by this procedure will be denoted as  $e_0$  hereafter.  $e_{\min}$  was determined by vibrating a mold using air-dry sand on a shaking table applying the pressure of  $1 \text{ kg/cm}^2$  on the top.  $e_{\max}$  was determined by spooning air-dry sand into a mold.  $e_{\min}$  and  $e_{\max}$  of Toyoura Sand by these methods are 0.61 and 0.96, respectively. Ishizawa, Nakagawa and Kurokawa (1977) also performed large diameter sand samplings at an alluvium deposit in Tokyo (site D). The methods for determining e,  $e_{\min}$  and  $e_{\max}$  are identical to those for site C. At a site in a hydraulic fill named as Ohgishima in Yokohama city (site I), Saito (1977) performed sand samplings

			(see I	(TI)					
		•			Dynamic	Triaxial C	Fest Cc	ndition	
Site	Sand Sampling	Void Katio Measurement	e <sub>min</sub> Measurement	e <sub>max</sub> Measurement	$\left( \log/cm^2 \right)  F $	requency for for	$\left. \begin{array}{c c} DA \\ \text{or} & R_l \\ (\%) \\ (\%) \end{array} \right _{(\varsigma)}$	Specimen bcm, hcm)	References
Site A (in Tokyo, along Tokyo Bay) Alluvial and Reclaimed	Modified Bishop-type sand sampler; the liner is $5.3 \text{cm}\phi$ and $65 \text{cm}\ell^{*0}$	<i>er</i> ; estimated in situ void ratio by Eq. (3)	Tamping mold with air-dry sand**) (0.64)	Lightly pouring air-dry sand into mold**) (0.96)	$=\sigma_{v}'=0.2$	1.0	9	5 <b>¢</b> , 10h	This Investigation *) Hanzawa and Matsuda (1977) **) Yoshimi and Tohno (1972)
Site B (in Shikoku, along Setonaikai Sea) Alluvial and Reclaimed	Twist sand sampler; the liner is 7 cm \$\$ and 80 cm \$\$	er';average void ratio in the liner before freezing	Identical	to Site A	$=\sigma_{v}'=$ 0.45~ 1.75	0.5	വ	7 <i>ф.</i> 14h	This Investigation *** <sup>3</sup> Ogura et al. (1978)
Site C (in Niigata City, along Shinano River) Alluvial and Reclaimed	Large diameter sand sampling; the liner is 20cm¢ and 100cml;	$e_o$ ; void ratio of thawed triaxial specimen at $\sigma_o'=$ 0.2kg/cm <sup>2</sup>	Vibrating mold using air-dry sand on shaking table with 1kg/cm <sup>2</sup> being applied on the top (0.61)	Spooning air-dry sand into mold (0.96)	$\begin{array}{c} 1.5 \\ (\sigma_{\bullet}' = \\ 0.3 \sim 1.15) \end{array}$	1.0	2	5 <i>ф</i> , 10h	Ishihara (1976, 1977) Ishihara and Silver (1977)
Site D (in Tokyo) Alluvial		Identical to	Site C		$\begin{array}{c} 0.5(\sigma_{\bullet}'=\\ 0.265 \widetilde{\sim}\\ 0.610) \end{array}$	1.0	2	5 <i>ф</i> , 10h	Ishizawa, Nakagawa and Kurohara (1977)
Site E (in Yokohama, along Tokyo Bay) Reclaimed	Identical to Site A		1		$=\sigma_{0,37}^{*'=}$ 0.77	1.0	9	5 <i>ф</i> , 10h	This Investigation
<u>Site F (in Tokyo, along Tokyo Bay)</u> Alluvial	Thin-wall sampling with enough cares	1	]	1	$ \begin{array}{c} 0.5, 1.0 \\ (\sigma_{*}'=0.24 \\ \sim 0.65) \end{array} $	1.0	9	5 <i>ф</i> , 10h	This Investigation
Site G (in Tokyo along Tokyo Bay) Alluvial and Reclaimed		Identical to	Site A		$= \frac{\sigma_{v'}}{0.8} = \frac{1.14}{1.14}$	0.5	9	5 <i>ф</i> , 10h	This Investigation
<u>Site H (Kawagishicho</u> <u>Niigata</u> City) Alluvial and Reclaimed	, Identical to Site A	ی ع	Tamping mold using air-dry sand and applying pressure of 1 kg/cm <sup>2</sup> on the top (0,60)	Average by two method; Kolbuszewski (1948) and Tanimoto (1975) (0. 94)	1	1		l	JSSMFE (1976)
Site I (Oh-gi Shima) Reclaimed	Identical to Site A	C.F.	Identical	to Site H	1	!	1	1	Saito (1977)
<u>Site J</u> (in Yokohama, <u>along</u> Tokyo Bay) Reclaimed	Frozen Column Method making frozen $5ml$ , $40 \text{ cm}\phi$ large column in ground	;Void ratio of frozen specimen	The Yoshimi-an (0.62)	ld-Tohno method (0.98)	1		1	I .	Yoshimi, Hatanaka and Oh-oka (1977), Hatanaka (1977)
(NOTE) The nur	nbers in ( ) represent t	he maximum and	minimum void ra	tios of Toyoura Sa	nd determin	ied by each	n metho	. þ	

Table 1. List of sand samplings and dynamic triaxial tests

48

# TATSUOKA ET AL.

using the modified Bishop-type sand sampler. The methods for determining e,  $e_{\min}$  and  $e_{\max}$  were identical to those for site H (Kawagishi-cho). And at a hydraulic fill along Tokyo Bay in Yokohama city (site J), a frozen column method was utilized by Yoshimi, Hatanaka and Oh-oka (1977) and Hatanaka (1977). In this method, a large scaled frozen column of sand, around 5m in length and around 40cm in diameter, was made in the ground and this was pulled out with a force of 5 tons or more to the ground. Small pieces of frozen specimen were cut from the large frozen column and their void ratios were measured with being kept frozen. It was confirmed by them from other basic experiments that void ratios determined by the method described above are almost identical to in situ values of void ratio.  $e_{\min}$  and  $e_{\max}$  were determined by the Yoshimi-Tohno method.  $e_{\min}$ and  $e_{\max}$  of Toyoura Sand by them are 0.62 and 0.98, respectively. It is seen from Fig.6 that there is a general trend showing that  $D_r - D_r^*$  decreases with the increase in  $D_{50}$ . Neverthless, a scatter shown in Fig.6 is too large for Eq. (2) to be used in precisely evaluating relative densities of various sands with a large range of  $D_{50}$ . Especially for silty sands which include a large amount of fine soils, it is obvious that relative densities are usually underestimated by Eq. (2).

One of the reasons which cause a large scatter in the data shown in Fig. 6 may be variations in densities of sands during sampling and handling operations. Except the frozen column method by Yoshimi, Hatanaka and Oh-oka (1977), there is a possibility that loose sands density and dense sands loosen at the time of pushing liners into sand deposits (Marcuson, Cooper and Bieganousky, 1977). Neverthess, it is likely that these variations in densities are not a main reason for a large scatter in  $D_r$ - $D_r^*$  for the same value of  $D_{50}$ . This is because it was found by the authors that possible variations in densities due to sampling and handling were much less that the scatter in  $D_r$ - $D_r^*$  in Fig. 6. To present authors, It is likely that a main reason for a large scatter in  $D_r - D_r^*$  is that N-values can be largely affected by other factors than  $D_r$ ,  $\sigma_v'$  and grading. One of these factors may be the in situ earthpressure coefficient at rest  $K_0$  (Saito, 1977). However, all samplings referred to in this study are performed at newly hydraulically reclaimed fills and alluvial Therefore, in this study,  $K_0$  can be estimated to be around 0.5 on past experideposits. Therefore, the variation in  $K_0$  may not be the main reason for a large scatter in ences.  $D_r - D_r^*$ . Other factors affecting  $D_r - D_r^*$  may include fabrics of soils, static and dynamic stress-strain-time histories, inhomogeneity of soil in a sampler or so. As further investigations are necessary to clarify the effects of these factors on N-values, it can be concluded that it is very difficult at present to estimate in situ relative density from standard penetration resistances.

As to item (2), the standard method of measuring the values of  $e_{\max}$  and  $e_{\min}$  have not been established in Japan so far. Several methods have been proposed by different researchers, and it is well-known that the values for silty sands depend on the method employed significantly. Therefore, it is difficult in Japan to determine uniquely the relative densities of silty sands even when samples are given. It can be seen from Table 1 that the values of  $e_{\max}$  and  $e_{\min}$  for an identical sand (Toyoura Sand) are different among different methods. This may be one of the reasons which cause a scatter in the data shown in Fig. 6.

Finally, as to item (3), it is necessary that the relationship between dynamic shear strength and relative density  $D_r$  be established for undisturbed specimens. For reconstituted specimens, Lee and Fitton (1969) and Seed and Idriss (1971) show that there is a variation in dynamic shear strength for an identical relative density with the variation in  $D_{50}$ . In this study, available data of undisturbed specimens were utilized to examine whether there is a correlation between dynamic shear strength and  $D_r$  as follows. Fig. 7 shows typical test results of undrained cyclic triaxial tests on undisturbed specimens which were obtained from one liner. These samples were obtained from site G which is close to site

A. The methods for sampling and determining  $e_{\min}$  and  $e_{\max}$  are identical to those for site A, and e is  $e_0$ . All of the tests referred to in this study were performed on specimens made from samples which were made frozen at the sites if the sample did not include a large amount of fine soils. This avoided disturbances caused during transportation from the site of sampling to the laboratory. Silty samples, however, were not frozen in order to avoid the disturbance due to volume expansion caused by freezing. In Fig. 7,  $\sigma_{dp}/2\sigma_c'$ is stress ratio where  $\sigma_{dp}$  is dynamic axial stress in single amplitude,  $\sigma_c'$  is effective confining pressure at dynamic triaxial testing and  $N_c$  means the number of loading cycles at which the state of initial liquefaction or a certain value of dynamic axial strain amplitude is observed. In this study, the dynamic shear strength in dynamic triaxial tests is defined as

$$R_l = (\sigma_{dp}/2\sigma_c') \tag{4}$$

which is the stress ratio  $(\sigma_{dp}/2\sigma_c')$  at the number of loading cycles  $N_c=20$  where the amplitude of axial strain in double amplitude (DA) becomes 5 or 6 percent. The values of  $R_i$  used in this study were read from such figures as Fig.7. In general, to obtain a value of  $R_i$ , three to six specimens obtained from one liner were tested. Of course, the definition



Fig. 7. Typical test result of dynamic triaxial test on undisturbed sandy specimens from site G



Fig. 8.  $R_l$  and  $D_r$  relation of undisturbed specimens from site A



Fig. 9.  $R_l$  and  $D_r$  relation of undisturbed specimens from site B



of strength as a function of the number of loading cycles and amplitude of axial strain should depend on the purpose of the study; for this research, the definition of Eq. (4) was considered adequate. Effects of changes in  $N_c$  and in amplitude of axial strain will be considered in future studies. It was found that the difference of  $R_l$  between for DA =5% and for 6% is quite small (3% at largest). Therefore,  $R_l$  for DA = 5% and  $R_l$  for DA = 6% can be considered to be able to utilize for the same analysis. And in all of the tests referred to, the Skempton's *B*-values were larger than 0.96. Note that except the values of isotropical confining pressure  $\sigma_c'$  and frequencies of cyclic loading the dynamic triaxial tests referred to in this study were performed by the almost same method using the almost same apparatus. The frequency of cyclic loading for the specimens from the sites

A, C, D, E and F is 1.0Hz and that for the specimens from the sites B and G is 0.5Hz. (The data for the sites E and F will be shown later.) The triaxial specimens from site B are 7cm in diameter and 14cm in height and the others are 5cm in diameter and 10cm in height (see Table 1). Fig. 8 shows the relationship between  $R_i$  defined by Eq. (4) and measured in situ relative density  $D_r$  for site A. Fig. 9 is a similar one for site B. Obviously, there is not a high correlation between two values for both sites. The relationship shown by solid lines in Figs. 8 and 9

$$R_l = 0.0042 D_r$$
 (5)

was derived from the data of reconstituted clean sands made by an almost identical method. This is shown in Fig. 10. It is seen from Fig. 10 that there is a rather unique relationship between strength  $R_i$  and relative density  $D_r$  for several clean sands. Eq. (5) was also proposed by Ishihara (1977) on the basis of Japanese data. Fig. 11 is the summary of the relationship between  $R_i$  and  $D_r$  for undisturbed specimens. It is obvious that there is no correlation among the data. To examine whether the variation in  $D_{50}$  is a main cause for a large scatter in the data in Fig. 11 or not, a parameter  $DR_i$  was defined as

$$DR_{I} = R_{I} - 0.0042 D_{r} \tag{6}$$

Fig. 12 shows the relationship between  $D_{50}$  and  $DR_{l}$  for the data shown in Fig. 11. It is seen from Fig. 12 that there is not a high correlation between  $DR_{l}$  and  $D_{50}$ . From Figs. 11 and 12, it is obvious that even if relative density could be estimated precisely, it is still difficult to estimate undrained cyclic triaxial strength from estimated relative density on the basis of the data shown in these figures. There may be several reasons for the large scatter in  $R_l$  in Fig. 11 or  $DR_l$  in Fig. 12. It was found that the differences in the methods of measuring e,  $e_{max}$ , and  $e_{min}$  cause smaller variations in  $DR_{l}$  than the observed scatter in  $DR_t$ . For specimens from sites A and B, isotropical effective confining pressures  $\sigma_c'$  at cyclic tests were identical to in situ effective overburden pressure  $\sigma_v'$ . But for specimens from sites C and D,  $\sigma_c'$  was different from  $\sigma_v'$ . This may cause some variations in  $R_i$ . However, it is obvious that this is not a main cause for the scatter in  $DR_{l}$ . It is likely that a main cause for the large scatter in  $DR_i$  may be that undrained cyclic strength  $R_i$ can not be related uniquely with relative density. Fig.13 shows the relationship between fine contents and the ratio of  $R_i$  of undisturbed specimens from site A to  $R_i$  of reconstituted specimens which were made from completely disturbed soils obtained from the undis-The reconstituted specimens were made by raining de-aired soil into a turbed specimens. mold fulfilled with de-aired water and had the equal relative densities to those of undisturbed specimens. It is seen from Fig. 13 that the differences in  $R_{l}$  for equal densities between undisturbed specimens and reconstituted specimens are considerable large in this This has been also reported by Ishihara and Tanaka (1974), Seed, Mori and Chan case. (1975) and Mulilis, Mori, Seed and Chan (1977). This means that there are some other unknown factors causing a scatter in  $R_i$  and in  $DR_i$ . Ladd (1974, 1976) and Mulilis, Chan and Seed (1975) has reported that one of these reasons is the fabric of sand. They showed that dynamic shear strength of reconstituted sands are greatly affected by the method of sample preparation. The variation in dynamic shear strength due to the variation in fabric for the same density may also be possible in in situ dynamic shear strengths, as shown in Fig. 13. Therefore, it is evident that relative density is not a unique parameter which determines the dynamic shear strength of sand.

In summary, it is evident that with the present knowledges it is extremely difficult to estimate undrained cyclic strength  $R_t$  of various sands by the A-method using standard penetration resistances,  $\sigma_{v'}$  and other factors within the limit of errors allowable for engineering purposes.

# A NEW SIMPLIFIED METHOD FOR EVALUATION OF UNDRAINED CYCLIC STRENGTH FROM STANDARD PENETRATION RESISTANCES (B-METHOD)

The B-method shown in Fig.1 is a more direct method than the A-method as described below. First, it is logical that in situ dynamic shear strength is in general related to several factors such as N-values, overburden effective pressure,  $\sigma_v'$ , lateral earth pressure  $\sigma_h' = K_0 \sigma_v'$ , grading properties and strain or stress histories. As for parameter  $K_0$ , the value of 0.5 can be assumed for all deposits examined in this study. To account for the effects of  $\sigma_{v}$  on N-values, Eq. (2) was adopted in correlating  $R_{i}$  with  $\sigma_{v}$ , N and gradings of



Fig. 14.  $R_l$  and  $D_r^*$  relation (summarized)



sampler. Also shown is the line representing the equation

$$R_l = 0.0042 D_r^* \tag{7}$$

This can be derived by substituting  $D_r = D_r^*$  into Eq. (5). The data for  $\sigma_c' = 0.5$  to  $2.5 \text{ kg/cm}^2$  from Castro (1975) are included in Fig. 14 in which  $R_{\mu}$ for  $N_c=20$ ,  $R_{l_{20}}$  were converted from  $R_l$  for  $N_c$ =10,  $R_{l_{10}}$  as  $R_{l_{20}} = R_{l_{10}}/1.15$ . Obviously, it is seen from Fig. 14 that there is no correlation between  $R_i$  and  $D_r^*$ . Castro (1975) has reported that the liquefaction of laboratory samples extracted from zones of sand having a high penetration resistance is little better than that of samples extracted from zones of low penetration resistance.



relation (summarized)

54

## TATSUOKA ET AL.

He suggested that this is due to a loosening of the dense sand during the sampling process. The data of such dense sands by Castro (1975) are shown by three points  $D_r^*$  of which are larger than 100. However, it can be assumed that the effects of such loosening may be relatively small for the sand deposits referred to in this study. This is because all the specimens referred to in this study were extracted from loose or medium sandy deposits which have  $D_r^*$  less than 100. Furthermore, it should be noted that  $D_r^*$  or N-values can be largely affected by grain size. This means that a large  $D_r^*$  or a large N-value may be caused by that the zones are gravelly and may not be caused by high density. Therefore, it can be anticipated that there can be a relatively high correlation among  $R_i$ ,  $D_r^*$  and parameters which represent grading properties of sands. To find this correlation, a parameter was defined as

$$DR_{l}^{*} = R_{l} - 0.0042 D_{r}^{*} \tag{8}$$

in which  $R_l$  is measured dynamic strength by Eq. (4) and  $D_r^*$  is measured value by Eq. (2). Note that Eq. (8) is analogous to Eq. (6). Fig. 15 shows the relationship between  $DR_l^*$  and fines content FC for fine sands  $D_{50}$  of which are smaller than 0.3mm (Oh-hashi, Iwasaki and Tatsuoka, 1978). It can be seen from Fig. 15 that there is a good correlation between  $DR_l$  and FC. The average line can be represented by

$$DR_{l}^{*} = 0.0035 FC \tag{9}$$

in which FC is fines content in percentage. From Eqs. (8) and (9),

$$R_l = 0.\ 0042 D_r^* + 0.\ 0035 FC \tag{10}$$

For fine sands  $D_{50}$  of which are smaller than 0.3mm, approximate values of  $R_l$  can be estimated from  $D_r^*$  and FC using Eq. (10). For a wider range of  $D_{50}$ , FC is not a good parameter enoughly representing grading properties of sands. The mean diameter  $D_{50}$  can be a more general parameter than FC. Fig. 16 shows the summary of the data available at present. It can be seen from Fig. 16 that for a wide range of  $D_{50}$ , there is a high correlation between  $DR_l^*$  and  $D_{50}$ . The average line drawn in Fig. 16 appears to be a reasonable representation of the relationship between  $DR_l^*$  and  $D_{50}$ . This line was determined to fit the data as well as possible, but not to be too complicated compared with their scatter. Especially for  $D_{50}$  larger than 0.6mm, a constant value of  $DR_l^*$  was considered appropriate. This average line can be represented by

$$DR_{l}^{*} = -0.225 \log_{10}(D_{50}/0.35) \text{ for } 0.04 \le D_{50} \le 0.6 \text{ mm} \\ DR_{l}^{*} = -0.05 \text{ for } 0.6 \le D_{50} \le 1.5 \text{ mm} \end{cases}$$
(11)

From Eqs. (8) and (11),

$$R_{l} = 0.0042 D_{r}^{*} - 0.225 \log_{10} \left( \frac{D_{50}}{0.35} \right) \text{ for } 0.04 \le D_{50} \le 0.6 \text{ mm} \\ R_{l} = 0.0042 D_{r}^{*} - 0.05 \qquad \text{ for } 0.6 \le D_{50} \le 1.5 \text{ mm}$$

$$(12)$$

and

and

in which  $D_r^* = 21\sqrt{N/(\sigma_v'+0.7)}$ . For  $D_{50}$  ranging from 0.04 to 1.5mm, Eq. (12) can be available to estimate approximate dynamic shear strength  $R_l$  using  $D_r^*$  and  $D_{50}$ . It can be noted that for the same value of  $D_r^*$ ,  $R_l$  increases with the decrease in  $D_{50}$  in Eq. (12). This means that if Eq. (7) is used to estimate  $R_l$  from  $D_r^*$ ,  $R_l$  can be underestimated for finer sands. Therefore, it can be pointed out from the facts shown in the above that if liquefaction potentials are estimated directly from N-values without taking into account grading properties of a sand, liquefaction potential can be overestimated for finer sand. Eq. (12), which can be considered to be one of the best ones which fit the data available at present, has an advantage over the B-method as follows. In Eq. (12), factors affecting undrained cyclic strength such as fabrics of sands, static and dynamic stress-strain-time histories or so other than relative density can be considered to have been taken into account for in a



Fig. 19.  $\Delta R_l$  and  $R_{lmeasured}$  relation

Fig. 20.  $\Delta R_l$  and  $D_r^*$  relation

simple manner. This is because these factors also affect standard penetration resistances in the similar manner to undrained cyclic strength (Seed, 1976). This makes the B-method considerably simpler than the A-method.

To examine the validity of Eq. (12) with the data from which Eq. (12) was derived, a parameter was defined as

$$\Delta R_l = R_{l\,\mathrm{measured}} - R_{l\mathrm{esti\,mated}} \tag{13}$$

in which  $R_{lmeasured}$  is measured dynamic shear strength defined by Eq. (4) and  $R_{lestimated}$ is estimated dynamic shear strength by Eq. (12). The average value  $\mu$  of  $\Delta R_l$  for all the data used in this analyses, the number of which is 123, is 0.003 and the standard deviation  $\sigma$  of  $\Delta R_l$  for all the data is 0.058. The small value of  $\mu$  of 0.003 means that Eq. (12) is adequate for all the data used in the study. And it can also be pointed out that when Eq. (12) is used, some errors in estimated  $R_l$  can be involved. Further investigations are necessary to account for this uncertainty in evaluating liquefaction potential. Fig. 17 shows the relationship between  $\Delta R_l$  the uniformity coefficient  $U_c = D_{60}/D_{10}$  which was not taken into account in deriving Eq. (12). On the basis of the data shown in Fig. 17, it may be concluded that there is not a high correlation between  $\Delta R_l$  and  $U_c$  and that the effects of  $U_c$  on the correlation among  $R_l$ ,  $D_r^*$  and grading properties are relatively small compared with  $D_{50}$ . Figs. 18, 19 and 20 show the relationships between  $\Delta R_l$  and  $\sigma_v'$ ,  $R_{lmeasured}$  and  $D_r^*$ , respectively. In these figures, high correlations can not be observed.

This means that Eq. (12) is rather homogeneous for  $\sigma_{v}'$  from 0.2 to  $1.7 \text{ kg/cm}^2$ , for  $R_i$  from 0.15 to 0.4 and for  $D_r^*$  from 15 to 80. To obtain in situ dynamic strength from triaxial strength  $R_i$  defined by Eq. (4), some corrections are necessary. This problem is beyond the scope of this paper.

# CONCLUSIONS

On the basis of the data from sand sampling procedures and dynamic triaxial tests on undisturbed specimens, a new simple method for evaluation of dynamic shear strength of sands from N-values by standard penetration tests and  $D_{50}$ -values was proposed. This is represented by Eq. (12). This equation can be effective for normally consolidated reclaimed and alluvial deposits for  $\sigma_{v}'$  ranging from 0.2 to  $1.7 \text{ kg/cm}^2$  and for  $D_{50}$  ranging from 0.04 to 1.5 mm. With this equation dynamic shear strengths are evaluated higher for finer sands for the same value of  $D_r^*=21\sqrt{N/(\sigma_v'+0.7)}$ . This accords with past experiences with standard penetration tests. Another point to be noted in this method is that relative density  $D_r = (e_{\max} - e)/(e_{\max} - e_{\min}) \times 100(\%)$  is not used. This extremely reduces uncertainties in evaluating strength from N-values,  $\sigma_{v}'$  and other soil parameters. With refining sampling and soil testing methods and with increasing the amount of data available, Eq. (12) will be modified. But the principal form of Eq. (12) may not be changed.

## ACKNOWLEDGEMENTS

The principal part of this research project was conducted at the Public Works Research Institute, the Ministry of Construction, while the first author was a staff member of Ground Vibration Section of the institute. Extensive in situ soil surveys and dynamic shear tests have been conducted by the Kanto Regional Construction Bureau of the Ministry of Construction, Honshu-Shikoku Bridge Authority and Yokohama city. The whole authors express their cordial appreciation to the staff members concerned.

# NOTATION

DA = double axial strain amplitude in dynamic triaxial tests  $D_r$  = relative density =  $(e_{\text{max}} - e)/(e_{\text{max}} - e_{\text{min}}) \times 100(\%)$  $D_r^* = 21 \sqrt{N/(\sigma_v' + 0.7)}$  $D_{50} = \text{mean diameter (mm)}$  $DR_{l} = R_{l} - 0.0042 D_{r}$  $DR_{l}^{*} = R_{l} - 0.0042 D_{r}^{*}$  $\Delta R = R_{l \, \text{measured}} - R_{l \, \text{estimated}}$ FC = fines content (%)N-value=blow counts by the standard penetration test  $N_c$ =number of cyclic loading in dynamic triaxial test  $R_l$  = dynamic shear stength in dynamic triaxial test =  $(\sigma_{dv}/2\sigma_c')$  at  $N_c=20$  and for DA=5 or 6% $U_c = \text{uniformity coefficient} = D_{60}/D_{10}$ e = void ratio $e_F = \text{in situ void ratio from } \gamma_d$  by Eq. (3)  $e_{F'}$  = mean void ratio of unfrozen sand in the liner of the sand sampler  $e_0$  = void ratio of that triaxial specimens confined by the vacuum pressure of -0.2kg/cm<sup>2</sup>

 $e_{\max}$ ,  $e_{\min}$  = maximum and minimum void ratios

 $\sigma =$  standard deviation

- $\sigma_v' = in$  situ effective overburden stress (kg/cm<sup>2</sup>)
- $\sigma_c'$ =isotropic effective confining stress in dynamic triaxial test (kg/cm<sup>2</sup>)  $\mu$ =mean value

 $\sigma_{dp}$  = dynamic axial stress in sigle amplitude in dynamic triaxial test

# REFERENCES

- 1) Bishop, A.W. (1948): "A new sampling tool for use in cohesionless sand below ground water level," Géotechnique, Vol.11, pp. 125-131.
- 2) Castro, G. (1975): "Liquefaction and cyclic mobility of saturated sands," Journal of the Geotechnical Engineering Division, ASCE, Vol. 101, No. GT 6, pp. 551-569.
- 3) Finn, W. D. Liam, Pickering, D. J. and Bransby, P. L., (1971): "Sand liquefaction in triaxial and simple shear tests," Journal of SMF Div., ASCE, Vol.97, No. SM4, pp. 639-659.
- Gibbs, H. J. and Holtz, W.G. (1957): "Research on determining the density of sand by spoon penetration test," Proc., 4th International Conference on Soil Mechanics and Foundation Engineering, London, Vol.1, pp. 35-39.
- 5) Hanzawa, H. and Matsuda, E. (1977): "Density of alluvial sand deposits obtained from sand sampling," Proc. of Specialty Session No.2, 9th ICSMFE, Tokyo, pp.7-14.
- 6) Hatanaka, M. (1977): "Fundamental studies on undisturbed sampling of saturated sands by freezing," A Thesis for the Degree of Doctor of Eng., Tokyo Institute of Technology.
- 7) Ishihara, K. and Tanaka, Y. (1974): "Liquefaction of undisturbed sand including fines content," Proc., 9th Annual Meeting of JSSMFE, pp. 379-382 (in Japanese).
- 8) Ishihara, K. and Watanabe, T. (1976): "Sand liquefaction through volume decrease potential," Soils and Foundations, Vol.16, No. 4, pp. 61-70.
- 9) Ishihara, K. (1976): "Report of liquefaction tests of at the site of Shinanogawa water gate," Report to the Hokuriku Regional Construction Bureau, the Ministry of Construction (in Japanese).
- 10) Ishihara, K. (1977): "Simple method of analysis for liquefaction of sand deposits during earthquakes," Soils and Foundations, Vol. 17, No. 3, pp. 1-18.
- 11) Ishihara, K. and Silver, M.L. (1977): "Large diameter sand sampling to provide specimens for liquefaction testing," Proc., Specialty Session No.2, 9th ICSMFE, Tokyo, pp. 1-8.
- 12) Ishizawa, M., Nakagawa, S. and Kurohara, I. (1977): "Liquefaction test of undisturbed samples containing fines content," Proc., the 12th Annual Meeting of JSSMFE, pp. 397-400 (in Japanese).
- 13) Japanese Society of Soil Mechanics and Foundation Engineering (1976): Report on Earthquake Damage to Subground Streets and Structures, March (in Japanese).
- 14) Kolbuszewski, J. J. (1948): "An experimental study of the maximum and minimum porosities of sand," Proc., 2nd ICSMFE, Vol.11b, pp. 158-165.
- 15) Ladd, R. S. (1974): "Specimen preparation and liquefaction of sand," Jour. of GT Div., ASCE, Vol.100, No. GT 10, pp. 1180-1184.
- 16) Ladd, R. S. (1976): "Specimen preparation and cyclic stability of sand," Pre-print of ASCE Annual Convention and Exposition on "Liquefaction Ploblems in Geotechnical Engineering," pp. 199-226.
- 17) Lee, K.L. and Fitton, J.A. (1968): "Factors Affecting cyclic Loading strength of soil," Vibration Effects of Earthquakes on Soils and Foundations, ASTM, STP450, pp.71-95.
- Lee, K. L. and Seed, H. B. (1976): "Cyclic stress conditions causing liquefaction of sand," Journal of SMF Div., ASCE, Vol.93, No. SM1, pp. 47-70.
- 19) Meyerhof, G.G. (1957): "Discussion of session 1," Proc., 4th International Conference on Soil Mechanics and Foundation Engineering, London, Vol.3.
- 20) Marcuson III, W.F., Cooper, S.S. and Bieganousky, W.A. (1977): "Laboratory sampling study conducted on fine sands," Proc. of Specialty Session, No. 2, 9th ICSMFE, Tokyo, pp. 15-22.
- 21) Mulilis, J. P., Chan, C. K. and Seed, H. B. (1975): "The effects of method of sample preparation on the cyclic stress-strain behavior of sands," EERC-Report, Report No. EERC75-18, College of Engineering, University of California, Berkley.

- 22) Mulilis, J. P., Mori, K., Seed, H. B. and Chan, C. K. (1977): "Resistance to liquefaction due to sustained pressure," Journal of GT Div., ASCE, Vol.103, No. GT7, July, pp. 793-797.
- 23) Ogura, K., Imai, T. and Suzuki, K. (1978): "Twist-type sand sampler," Proc., 13th Annual Meeting of JSSMFE (in Japanese).
- 24) Ohashi, M. Iwasaki, T. and Tatsuoka, F. (1978): "A simplified procedure for assessing seismic liquefaction of silty sand deposits," Central American Conference on Earthquake Engineering, San Salvador, EI Salvador, Central America.
- 25) Saito, A. (1977): "Characteristics of penetration resistance of a reclaimed sandy deposit and their change through vibratory compaction," Soils and Foundations, Vol.17, No. 4, pp. 31-43.
- 26) Seed, H. Bolton, and Lee, K.L. (1966): "Liquefaction of saturated sand during cyclic loading," Journal of SMF Div., Proc., ASCE, Vol.97, SM9, pp. 1249-1273.
- 27) Seed, H. B. and Idriss, I. M. (1967): "Analysis of soil liquefaction: Niigata earthquake," Journal of SMF Div., ASCE, Vol 93, No. SM3, pp. 83-108.
- .28) Seed, H. B., Mori, K. and Chan, C. K. (1975): "Influence of seismic history on liquefaction of sands," Journal of GT Div., ASCE, Vol.102, No. GT 4, pp. 257-270.
- 29) Seed, H. B. (1976): "Evaluation of soil liquefaction effects on level ground during earthquakes," State-of-the-Art Report, Preprint of ASCE Annual Convention and Exposition on Liquefaction Problems in Geotechnical Engineering, Philadelphia.
- 30) Seed, H. B. and Idriss, I. M. (1971): "A simplified procedure for evaluating soil liquefaction potential," Journal of the Soil Mechanics and Foundations Division, ASCE, Vol.97, No. SM9, Sept., pp. 249-274.
- 31) Shibata, T. (1970): "Analysis of liquefaction of saturated sand during cyclic loading," Disaster Prevention Research Institute, Kyoto University, Research Report No. 13B, pp. 1-8.
- 32) Tanimoto, K. (1971): "Liquefaction potential of cohesionless soils based on laboratory test results," Proc., 6th Symposium on Soil Mechanics and Foundation Engineering, pp. 21-26 (in Japanese).
- 33) Tanimoto, K. and Iwasaki, T. (1975): "Method of measurement of minimum density of sand," Proc., 10th Symposium on Soil Mechanics and Foundation Engineering, JSSMFE, pp. 11-14.
- 34) Yoshimi, Y. and Tohno, I. (1972): "Statistical significance of the relative density," ASTM, Special Technical Publication No. 523.
- 35) Yoshimi, Y., Hatanaka, M. and Oh-oka, H. (1977): "A simple method for undisturbed sand sampling by freezing," Proc. of Specialty Session 2, ICSMFE, Tokyo, pp. 23-28.

(Received January 27, 1978)

58