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### An Examination of Active Electromagnetic and Mechanical Suspension Control of Superconducting Maglev Vehicles

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In the continuing efforts toward the commercial operation of the superconducting magnetically levitated high speed ground transport (Maglev) system, in which vehicles travel at high speeds of over 500 km/h, methods of suppressing vehicle vibrations are being examined with respect to suitability for a public mode of transportation. Results will be presented on methods for suppressing vehicle vibrations of a Maglev train, examining techniques such as control of the primary suspension using electromagnetic forces output by a bogie-integrated linear generator, and a preview control of the secondary suspension by mechanical actuators using data transmitted from the front to the rear of the train.

Key Words: Maglev, vehicle vibration, electromagnetic suspension, preview control, ride comfort.

### 1. Introduction

In initial vehicle running tests, vibrations of the superconducting Maglev vehicle were controlled mainly focusing on the secondary suspension, and the control methods have been effective only for vibrations of relatively low frequencies at around 1 to 2 Hz corresponding to the natural car body vibration mode. The lightweight structure of the car bodies result in vibrations at around 4 to 5 Hz corresponding to the natural bogie vibration mode, and at other relatively higher frequencies that influence the ride comfort.

A device called a linear generator, which was developed and temporarily integrated into an existing bogie of the Maglev system for trial examination, generated on-board power while also producing additional electromagnetic forces that could be used in the control of the primary suspension. This device has previously been demonstrated in full-scale vehicle experiments to effectively apply electromagnetic damping directly to the primary suspension, and reduce vibrations of relatively higher frequencies that are otherwise difficult to reduce by controlling only the secondary suspension [1].

The Maglev train set has an articulated bogie arrangement to provide a low center of gravity and improved magnetic shielding performance. The bogies are evenly spaced along the train set. In addition, because of the interactions of electromagnetic forces in the primary suspension, each bogie of the Maglev train set is subjected to nearly the same external disturbance, with practically equal time differences between consecutive bogies. Utilizing these properties, techniques for preview control of the secondary suspension were previously examined that measure external disturbances at the front of the Maglev train set and feed the data to the rear of the train, to enhance the vehicle ability to efficiently minimize the impact of deviations in the guideway ground coil alignment [2].

The aforementioned previous work of Reference [1] reported results of controlling only the primary (electromagnetic) suspension. Reference [2] considered preview control of only the secondary (mechanical) suspension. A previous report did discuss some results of a study combining control methods of primary and secondary suspension components, but considered a linear quadratic (LQ) feedback control in the secondary suspension component, without feed forward elements of a preview control method [3]. This report presents results of a new study on a method for reducing vehicle vibrations of the superconducting Maglev train, examining the vibration control of the primary suspension using electromagnetic forces output by a bogie-integrated linear generator, combined with the preview control of the secondary suspension. Effective



Fig. 1: View of the superconducting Maglev system.

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Fig. 2: Mechanism of additional upward force acting on the bogie, output by linear generator coils and used for vibration control.

implementation of these vibration reduction methods on Maglev vehicles are expected to improve ride comfort, and eventually lead to the reduction of construction costs by enabling the relaxation of the limits of tolerated irregularities in the guideway alignment, and the reduction of management costs by minimizing guideway maintenance. Such cost reductions are expected to outweigh the increase in vehicle costs due to installation of vibration control systems.

### 2. Mechanism of the Bogie-Integrated Linear Generator Device in the Control of the Primary Suspension

As shown in the cross-sectional view of the superconducting Maglev system in Fig. 1, levitation/guidance coils and propulsion coils are installed on the sidewalls of a concrete guideway. The vehicle is equipped with superconducting magnet (SCM) coils and linear generator coils attached to the outer vessel surface of the SCM as part of the Maglev bogie-integrated linear generator device that generates power in the traveling vehicle using the harmonic magnetic fields in the levitation/guidance coils. This device can also be used to generate additional electromagnetic forces in the primary suspension to be used as control forces in reducing vehicle vibrations. The principles of additional electromagnetic forces output by the linear generator are shown in Fig. 2 [4]. The equivalent configuration of the linear generator coil for the function of generating additional forces is expressed in Fig. 2(a). Electrical current of amplitudes much smaller than that in the SCM coil is run through the linear generator coils. The resulting change in magnetic flux causes the already existing current in the levitation/guidance coil to increase slightly, indicated by the wide circular arrows in Figs. 2(a) and 2(b). These additional currents generate additional forces indicated by the smaller additional arrows in Fig. 2(c), resulting in additional upward force acting on the bogie. Likewise, additional downward force acting on the bogie can be generated by reversing the direction of the current flowing in the linear generator coil. By varying the amplitude and direction of the current in the linear generator coils according to the vertical motion of the vehicle bogie, this device can be used to control vertical vehicle vibrations.

This method has the advantage of requiring no additional systems solely for the purpose of generating electromagnetic forces. Furthermore, because the magnetic force is generated electrically, this method has minimal delay in response for high frequency ranges of vibration, in comparison to conventional methods using hydraulic or pneumatic systems [1]. Full-scale vehicle running tests on the Yamanashi Maglev Test Line confirmed the principles of magnetic forces output by the bogie-integrated linear generator device in the Japanese fiscal year 2001. Vehicle running tests then confirmed the ability of the linear generator device to control vibrations using the generated forces in the fiscal year 2004 [5].

### 3. Analyses of Vehicle Dynamics

### 3.1 Vehicle model used in the computations

A vehicle model of a three-car train set for vertical and pitching motions with a total of 14 degrees of freedom was used, as shown in Fig. 3. The primary suspension between the bogie and guideway surface consists of electromagnetic spring characteristics resulting from interactions between the superconducting magnets and ground coils. The spring characteristics of the vertical and pitching motions are coupled with each other. The magnetic spring acts in equal distribution along the length of the bogie from front to rear.



Fig. 3: Vehicle model used in the computations.

However, for purposes of optimizing computations, equivalent spring characteristics were approximated by concentrating the springs at two positions, one on the front and the other on the rear of the bogie. The secondary suspension between the car body and bogie consists of air springs that were approximated using a damper and a spring connected in parallel. Actuators for vibration control were added to the secondary suspension of the middle and rear cars (No. 2 and 3) and were assumed to have ideal operating properties with no time delay. In the primary suspension control model, the forces output by the bogie-integrated linear generator were used in all four bogies as damping forces in the vibration control.

The aforementioned magnetic forces output by the linear generator were assumed to be ideal, and delays in response were not considered. Furthermore, these magnetic forces of the linear generator are assumed to be equally distributed along the length of the bogie surface, such that the force at any longitudinal position on the bogie surface is of the same magnitude and same direction at any given time. For example, if an upward control force acts on the front end of a bogie at a given instance in time, an upward force of equal magnitude simultaneously acts on the rear end. Therefore, this force is assumed to have no influence on the bogie pitching motion. In the computation model, an equivalent vertical control force was concentrated on one point at the center of mass of each of the four bogies. Although the force only controls the vertical motion, the pitching vibrations are expected to be much smaller than the vertical vibrations in the passive case, making vertical control a priority. The vehicle traveling speed was set to a constant 500 km/h, which is a priority in this study, because the superconducting Maglev system is designed to travel long distances for a majority of the time at this speed. Furthermore, the electromagnetic spring characteristics of the primary suspension do not vary greatly at high speeds greater than 300 km/h [6].

### 3.2 Vehicle model parameters

The vehicle model parameters used in the computations are shown in Table 1. The values are based on those used in Reference [3].

Table	1:	Vehicle	model	parameters

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Parameter	Value				
$m_c$ [kg]	$14.0 \times 10^{3}$				
$m_b$ [kg]	$6.0 \times 10^3$				
$I_c [\text{kg} \cdot \text{m}^2]$	$82.0 \times 10^4$				
$I_b [\text{kg} \cdot \text{m}^2]$	$13.2 \times 10^{3}$				
$k_{z}$ [N/m]	$0.4 \times 10^{6}$				
$k_{mz}$ [N/m]	$4.7 \times 10^{6}$				
$k_{m\theta}$ [N·m/rad]	$1.0 \times 10^{7}$				
$c_{z}$ [N·s/m]	$1.0 \times 10^4$				
$l_{ac}$ [m]	8.8				
$l_{ab}$ [m]	2.03				



Fig. 4: Ride comfort filter and frequency shaping functions  $\overline{Q}(j\omega)$ ,  $\overline{R}(j\omega)$ .

### 4. Suspension Control Systems

# 4.1 Frequency-shaped optimal preview control of the secondary suspension

When the objective is to improve vehicle ride comfort, optimal control laws usually include a evaluation function based on the car body acceleration. Because human perception of vibrations differs according to the frequency, vibrations can be efficiently reduced by evaluating acceleration data modified by frequency shaping techniques, resulting in a control method that takes ride comfort factors into consideration. In this study, a frequency shaping function  $Q(i\omega)$  was derived, with gain characteristics based on the ride comfort level curve shown in Fig. 4, used by the former Japanese National Railways to define frequency-dependant human sensitivity to vibrations. In order to suppress the actuator output at high frequencies, a frequency shaping function  $R(j\omega)$ was also applied to the control input. The shaping factor gain increases from around 10 Hz to 30 Hz, where the ride comfort level curve drops, and levels off at around 30 Hz, in effect a high pass filter. The state equation for  $Q(j\omega)$  can be expressed using the input Y, state  $X_q$ , and coefficient matrices  $A_q$ ,  $B_q$ ,  $C_q$ , and  $D_q$ :

$$\dot{X}_q = A_q X_q + B_q Y$$

$$Y_q = C_q X_q + D_q Y$$
(1)

In the same manner, the state equation for  $\overline{R}(j\omega)$  can be expressed as:

$$X_r = A_r X_r + B_r u$$
  

$$Y_r = C_r X_r + D_r u$$
(2)

The state equations for the vehicle model shown in Fig. 3 can be expressed as:

$$\dot{X} = AX + Bu + W\dot{x}_0$$

$$Y = CX + Du + Z\dot{x}_0$$
(3)

Here, X represents the state variables, Y the output used in Eq. (1), u the control input,  $\dot{x}_0$  the rate of change of the external disturbance  $x_0$  with respect to time, and A, B, C, D, and Z the coefficient matrices. By substituting Y in Eq. (1) with the output of Eq. (3), frequency shaping factors are applied to the output.

The state equations are discretized to construct an optimal preview control system [2]. Finally, an evaluation function J is used to derive feedback and feed-forward coefficients. This function evaluates values resulting from frequency shaping factors added to the output Y and the input u, and is expressed as:

$$J = \sum_{k=-M_{g}+1}^{\infty} \left\{ q \left[ \sum_{n=0}^{k-1} \overline{Q}(n) Y(k-n) \right]^2 + r \left[ \sum_{n=0}^{k-1} \overline{R}(n) u(k-n) \right]^2 \right\}$$
(4)  
$$= \sum_{k=-M_{g}+1}^{\infty} \left[ q Y_q^2(k) + r Y_r^2(k) \right]$$

Here, q and r are coefficient weighting matrices, and  $M_R$  is the number of preview steps. The optimal control input can be derived by solving the Riccati equation resulting from substituting the outputs of Eqs. (1) and (2) into Eq. (4). Considering real-time performance and redundancy in this study, the frequency-shaped optimal preview control system was implemented using decentralized controllers. The vehicle model for computations is divided up as shown in Fig. 5, such that a reduced-order sub-model unit exists now for each actuator, with two vertical degrees of freedom in each sub-model unit consisting of one car body component and one bogie component. A controller is designed independently for each sub-model unit. For example, the state variables of Controller No. 1 in Fig. 5 are the vertical velocities and relative displacements of the car body and bogie:

$$x_{controller|} = \left[ (\dot{z}_{c2}) (\dot{z}_{b2}) (z_{c2} - z_{b2}) (z_{b2} - z_{02r}) \right]^{T}$$
(5)

Decentralizing the control system results in four state variables as shown in Eq. (5), and greatly simplifies the computations in comparison to designing



Fig. 5: Model of decentralized controllers.

the controller using the full order of the entire model. For this decentralized controller model, the control system is designed by the methods described earlier in this section. Here, the evaluation function of this control model is based on Eq. (4) and expressed as follows:

$$J = \sum_{k=-M_{k}+1}^{\infty} \left\{ q_{1} \left[ \left( \sum_{n=0}^{k-1} \overline{Q}(n) \ddot{z}_{c2}(k-n) \right)^{2} + \left( \sum_{n=0}^{k-1} \overline{Q}(n) \ddot{z}_{c3}(k-n) \right)^{2} \right] + \left( q_{2} \left[ \left( z_{c2}(k) - z_{b3}(k) \right)^{2} + \left( z_{c3}(k) - z_{b3}(k) \right)^{2} + \left( z_{c3}(k) - z_{b3}(k) \right)^{2} + \left( z_{c3}(k) - z_{b4}(k) \right)^{2} \right] + r \sum_{i=1}^{5} \left( \sum_{n=0}^{k-1} \overline{R}(n) u_{i}(k-n) \right)^{2} \right\}$$
(6)

Equation (6) includes frequency shaping of vertical accelerations of cars No. 2 and 3 and control inputs, and coefficient weighting of relative displacements. Coefficient weighting of the relative displacements can prevent vertical physical limit stoppers from colliding between the car body and bogie when the vertical displacement becomes very large. In this study, in order to achieve the maximum effect of vibration control, a limit was set for the maximum root-mean-squared (RMS) value of the forces generated by each actuator, rwas set to a constant value, and  $q_1$  and  $q_2$  were varied to determine a combination of values that result in maximum improvement of ride comfort, within the defined limits of the actuator output. The weighting coefficients used in this study are shown in Table 2. Each car body and bogie was assumed to be symmetric in the longitudinal direction, such that the effective masses on which each controller acts consists of the front and rear halves of the bogie mass  $m_{bf} = m_{br}$  and car body No. 2 mass  $m_{cf} = m_{cr}$ . The rear car body mass is evenly distributed, such that  $m_{cf} = m_{cr} = m_c/3$ .

This decentralized control method is advantageous when considering real-time implementation, but does not take into consideration state variables of the bogie pitching motions. Consequently, the bogie pitching motion is not directly controlled using this method. However, the vertical motion at the front and rear of each bogie are controlled, resulting in the reduction of pitching motions for the frequencies that most greatly influence ride comfort. Vibrations of pitching motions increase slightly at certain frequencies, and such issues may need to be addressed in future work, but the influence of these vibrations on the ride comfort are very small and therefore considered not to be a problem within the scope of this study.

Table 2: Weighting coefficients used in frequency-shaped optimal preview control.

Coefficient	$q_1$	$q_2$	r
Value	10 <sup>7</sup>	10 <sup>10</sup>	1

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# 4.2 Maximum force control of the primary suspension using the linear generator device

As discussed in Chapter 2, the bogie-integrated linear generator device can generate additional electromagnetic forces that can be applied to the vibration control of the primary suspension. Reference [1] mentions that the forces output by this linear device are relatively small for generator the requirements vibration control of the primary suspension. In order to fully utilize the forces generated by the bogie-integrated linear generator device, the maximum possible force output by the linear generator device is used at all times, with the polarity of the force switched according to the polarity of the bogie vertical velocity as expressed in Eq. (7) [1].

$$F_{mz} = -sign(\dot{z}_b) \cdot f_{mz} \tag{7}$$

Here,  $F_{mz}$  represents the control force and  $f_{mz}$  the maximum possible vertical force output by the linear generator device. The computations assume that the bogie vertical velocity  $\dot{z}_b$  which is the control feedback variable is derived by using accelerometers to measure the acceleration of the vertical vibration of the bogie, then integrating this acceleration once to derive the absolute velocity. Equation (7) was added to the dynamic equations of the vertical motions of all four bogies in Eq. (3). The computations assume that the control force of each bogie can be applied independently of each other.

### 5. Model Guideway Irregularities for External Disturbance Input and Ride Comfort Levels

To assess the effectiveness of the vibration control method, irregularities in the vertical alignment of ground coils along the sidewalls of the guideway (vertical irregularities) were generated, and used as external disturbance input in time domain simulations. A transfer function was formed based on Reference [3], and a uniformly random number was used to compute



Fig. 6: PSD plot of guideway irregularities.

the vertical irregularities. This transfer function has the characteristic of flattening out at low frequencies in order to reduce the amplitude of vibrations in low frequency ranges. The power spectral density (PSD) of the vertical irregularities is shown in Fig. 6.

The ride comfort level, a quantitative index for passenger comfort based on the car body acceleration response to vertical irregularities, was used to confirm the performance of the vibration control in this study. This ride comfort level (denoted  $L_T$ ) is based on ISO 2631 and was devised by the former Japanese National Railways. To derive the  $L_T$  value, ride comfort filters based on frequency shaping curves are applied to the vehicle response in the form of the car body vibration acceleration, to account for human perception of vibrations. Next, the resulting value is divided by a reference vibration acceleration value  $a_{ref}$ . Finally, the logarithm of the RMS of this value is derived, and expressed in decibels (dB). The following equation was used in this study to compute the ride comfort levels [7].

$$L_T = 20\log_{10}(\alpha_w/a_{ref}) \quad [dB] \tag{8}$$

where

$$\alpha_w^2 = \int_0^\infty W^2(f) \cdot P_{xx} \cdot df$$

$$a_{ref} = 10^{-5} [m/\sec^2]$$
(9)

Here, W(f) represents the ride comfort filter, and  $P_{xx}(f)$  the car body vibration acceleration PSD. Since there are no regulations defining this filter for frequencies below 0.5 Hz, the weighting factor for 0.5 Hz was also used for the frequency range below 0.5 Hz.

### 6. Results

The following cases were studied as described in this chapter in the sections to follow:

Case 1: Frequency-shaped optimal preview control of secondary suspension.

Case 2: Maximum force control of primary suspension.

Case 3: Cases 1 and 2 combined.

## 6.1 Frequency domain computation results of the secondary suspension control

Time domain simulations were performed with the secondary suspension control, using the vertical irregularities described in the previous chapter. Vertical acceleration PSD plots of car body No. 2 were derived from the time domain response, and are shown in Fig. 7. The quantity of reduction of the average ride comfort level relative to the reference passive case is displayed in the legend of this figure. The car body PSD peak at around 1 to 2 Hz corresponding to the vertical motions of the car body is greatly reduced in Case 1 while the peak at around 4 to 5 Hz corresponding to the bogie vertical motions is only slightly reduced. While

previous studies [3] indicated that an optimal preview control method without applying frequency shaping functions (Fig. 4) results in vibrations of frequencies over 10 Hz becoming larger than in the passive case, Fig. 7 shows that the frequency shaping functions applied in Case 1 of this study was able to reduce these higher frequency vibrations to levels equivalent to those of the passive case. The resulting ride comfort level in Case 1 is over 3 dB lower than in the passive case.

# 6.2 Frequency domain computation results of the primary suspension control

Vertical acceleration PSD plots of car body No. 2 were derived from the time domain response for the maximum force control of the primary suspension, and are shown in Fig. 7. The vertical generated force  $f_{mz}$  in Eq. (7) was set to 2 kN, and applied to each of the four bogies. As defined at the beginning of this chapter, Case 2 represents the maximum force control of the primary suspension control alone, and Case 1 is the frequency-shaped optimal preview control of the secondary suspension alone. Again, the quantity of reduction of the average ride comfort level relative to the reference passive case is displayed in the legend of this figure. The car body PSD peak at around 1 to 2 Hz corresponding to the vertical motions of the car body has been reduced in Case 1 to about one-seventh of the passive case, while this peak was hardly reduced in Case 2. The peak at around 4 to 5 Hz corresponding to the vertical motions of the bogie is slightly reduced in Case 1, while notably reduced in Case 2, to about one-sixth of the passive case. Although the reduction ratio of the frequency peak at around 4 to 5 Hz in Case 2 with respect to the passive case is much smaller than the reduction ratio of the frequency peak at around 1 to 2 Hz in Case 1, the resulting effect on the ride comfort level is of the same order for both cases, over 3 dB







Fig. 8: Car body No. 2 center vertical acceleration PSD plots of Cases 1 and 3.

lower than in the passive case. These similar decibel values are a result of the ride comfort filter (Fig. 4) used to apply different weighting factors for different frequency ranges in the computation of the ride comfort level shown. Specifically, reduction of vibrations in the 4 to 8 Hz range is considered to have the greatest impact on human perception of vertical vibrations, and consequently influences the ride comfort level more than any other frequency range.

### 6.3 Combined primary and secondary suspension control

As defined at the beginning of this chapter, Case 3 combines Case 2, the maximum force control of the primary suspension, with Case 1, the frequency-shaped optimal preview control of the secondary suspension. Vertical acceleration PSD plots of car body No. 2 for Cases 1 and 3 are shown in Fig. 8. The PSD peak of car body No. 2 at around 1 to 2 Hz has been reduced in Case 3 to about one-seventh of the passive case, the same as that of Case 1. The peak at around 4 to 5 Hz is slightly reduced in Case 1, while significantly reduced in Case 3, to about one-fifteenth of the passive case. With respect to the passive case, the reduction of ride comfort level in Case 3 is slightly larger than the sums of the reductions of ride comfort levels in Cases 1 and 2. The improvement of the ride comfort level in Case 3 is considerably large, once again because of the reasons mentioned at the end of Section 6.2. Similar results were observed in the car body No. 3.

### 7. Conclusions

A study was conducted on the effectiveness of applying vibration control to the primary and secondary suspension components in a model of the vertical and pitching motions of the superconducting Maglev vehicle. Results confirmed that a frequency-shaped optimal preview control of the secondary suspension alone can improve ride comfort levels in the middle car body to nearly the same degree as the case of the maximum force control of the primary suspension alone. The vibration peaks at 1 to 2 Hz and at 4 to 5 Hz were considerably reduced by combining the primary and secondary suspension control methods, and the reduction of the ride comfort level with respect to the passive case is larger than the sums of the reductions of ride comfort levels of each control method applied alone.

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